

For each of the following statements, determine whether it is true or false and then prove your answer.

1. There is some $n \in \mathbb{N}$ such that $9n^2 < n^3 < 15n^2$.
2. There is some $n \in \mathbb{N}$ such that $n < n^3 < 4n$.
3. There is some $n \in \mathbb{R}$ such that $n < n^3 < 4n$.